

# SmartAIR – IFD / SDSC

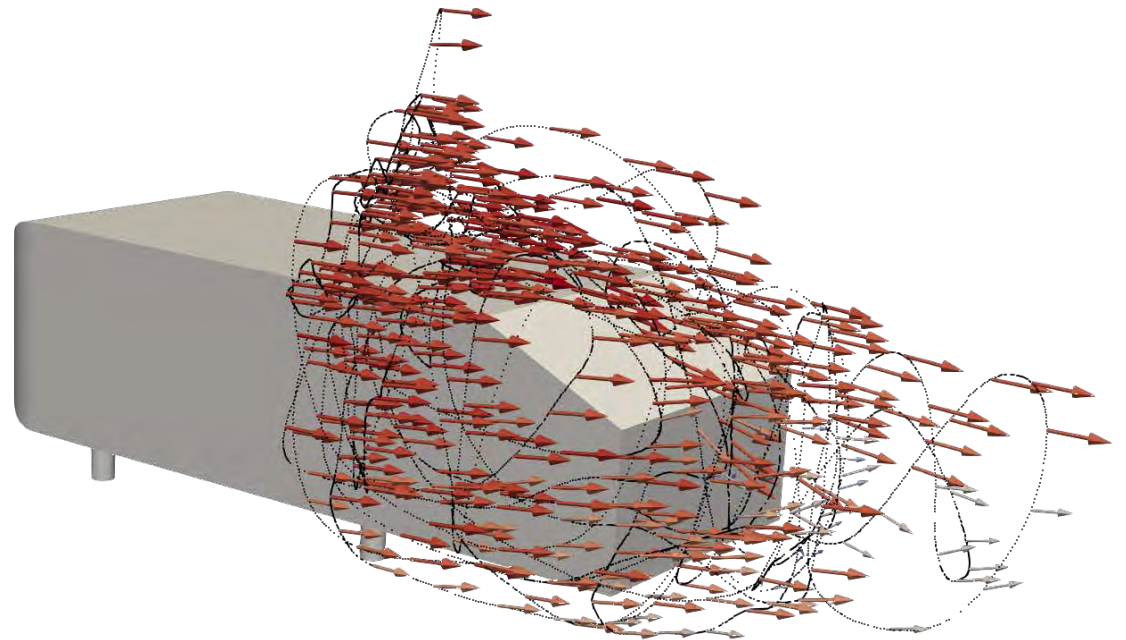
J. Humml, Prof. T. Rösgen, Institute of Fluid Dynamics, ETH Zürich

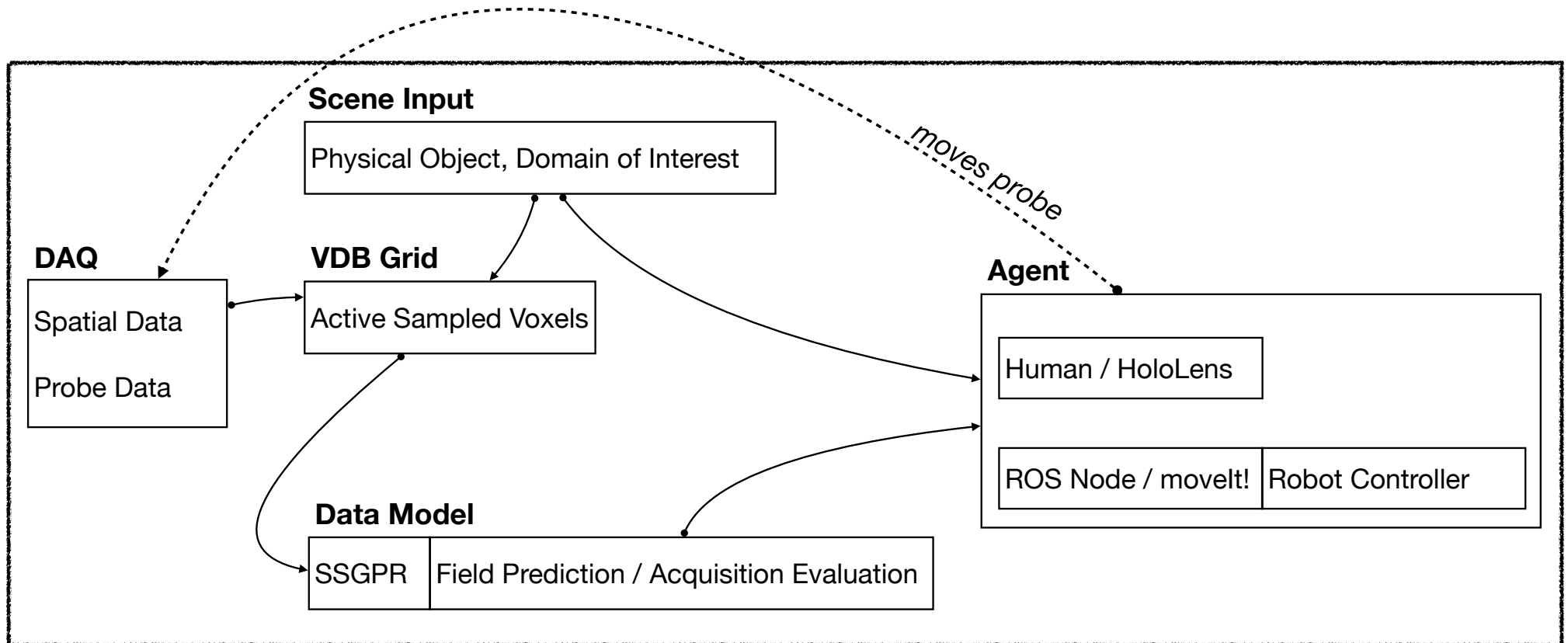
System	Data Sets
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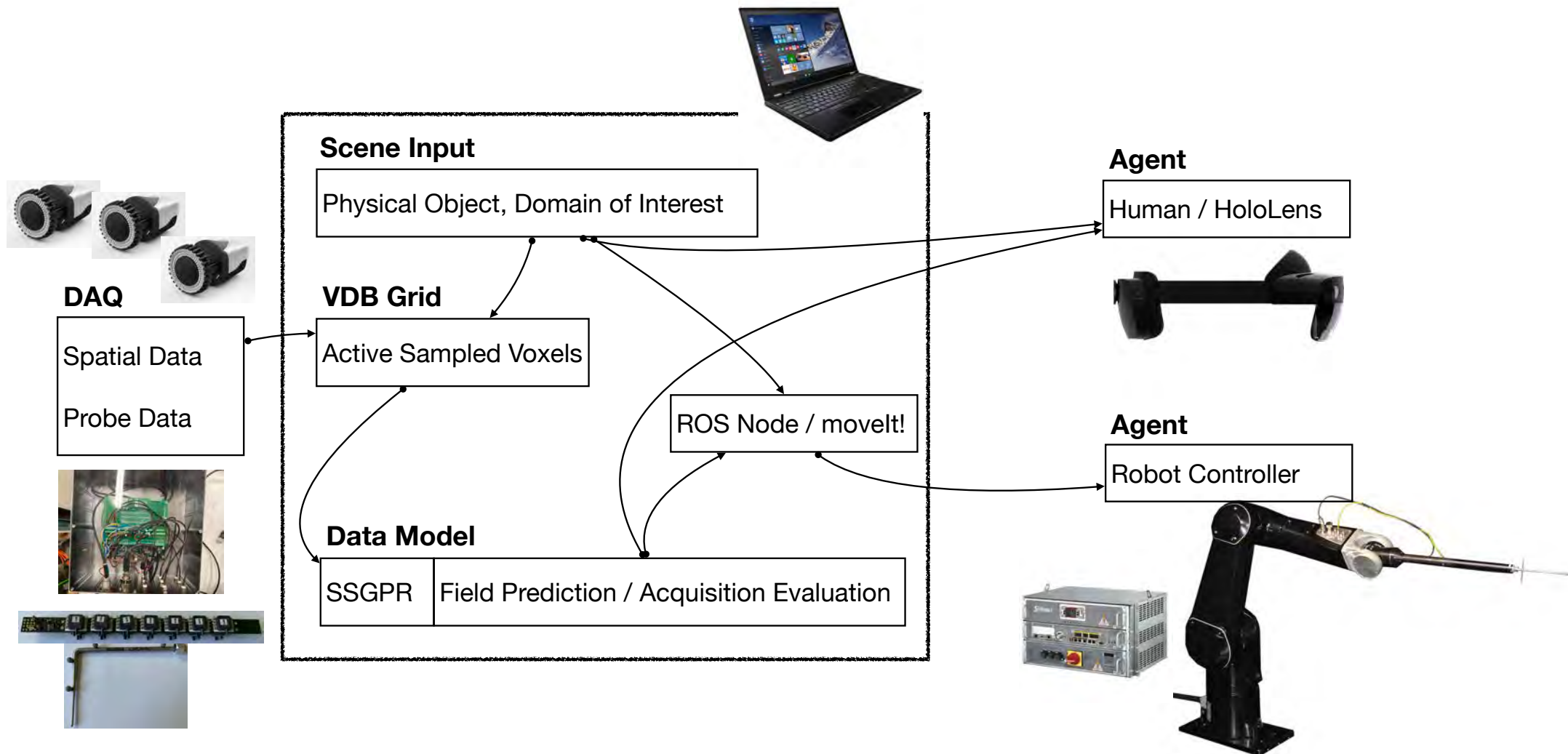
## Outline

### I. Current State of System

### II. Available Data Sets







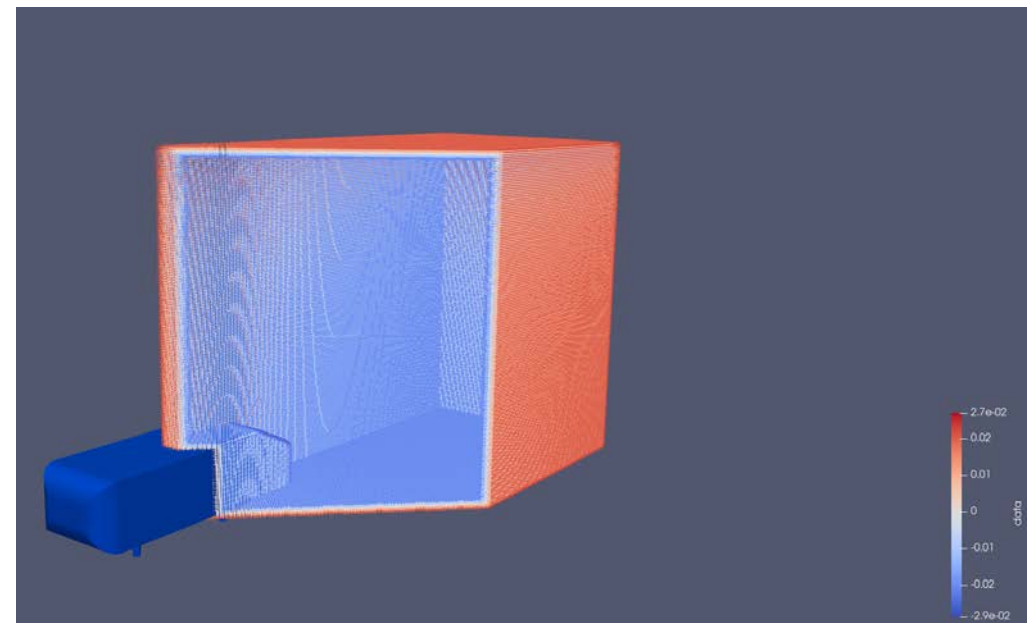
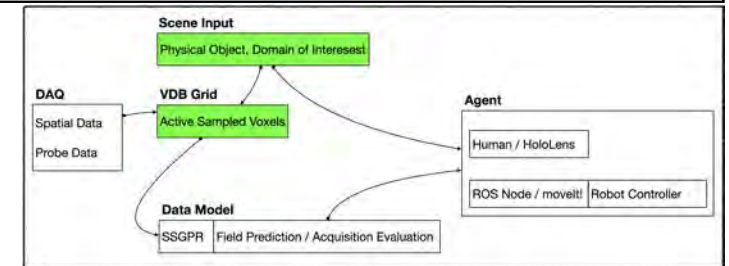


## Scene Input & VDB Grid

CAD files describing scene and domain of interest as input.

CSG operation creating B+ tree ([openvdb.org](http://openvdb.org)) of investigated volume.

Sampled data sparse, prediction of field dense.



*Cut through signed distance field of investigated volume*

## Scene Input & VDB Grid

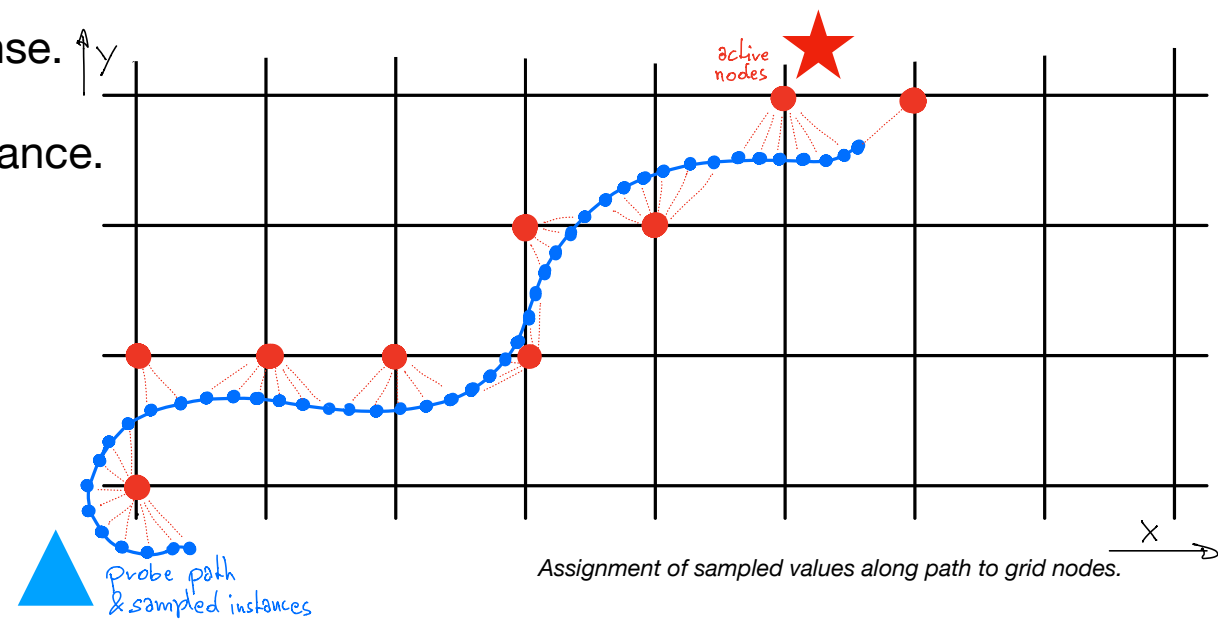
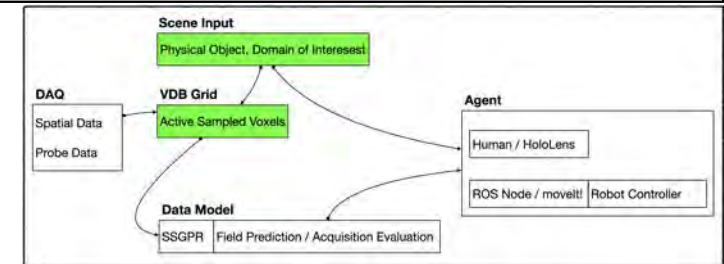
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Welford's online algorithm for mean and variance.

Smoothing of data for further processing.



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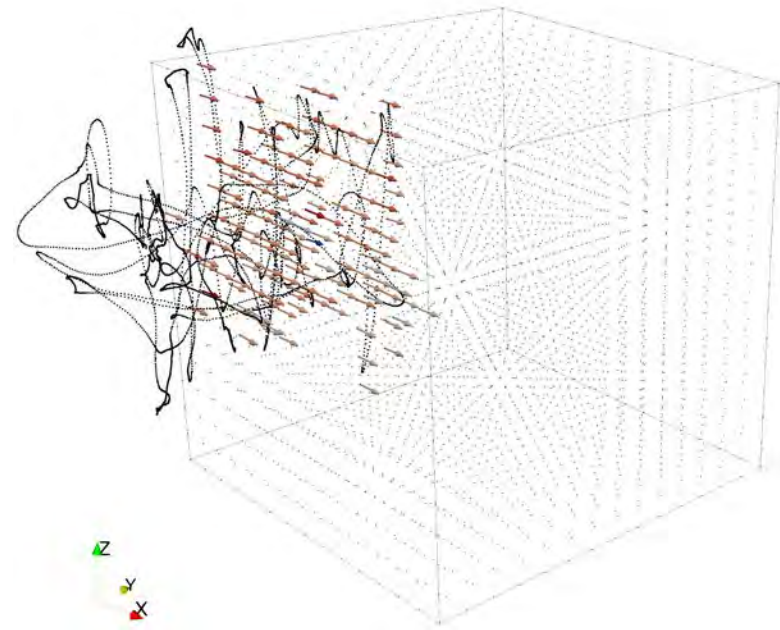
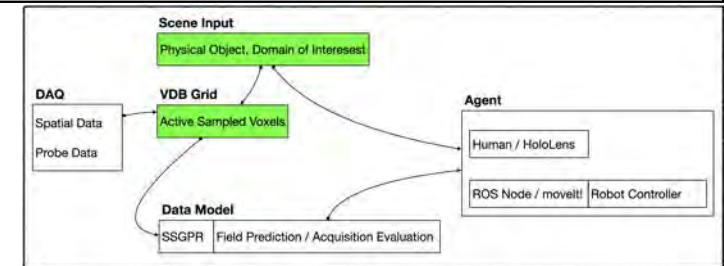
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*Assignment of sampled values along path to grid nodes.*

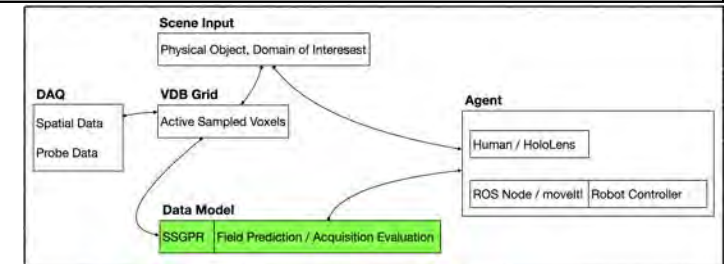
## Data Model

Model field properties:

- pressure (scalar field)
- velocity (vector field)

Gaussian Process Regression / Kriging with anisotropic Radial Basis Function (RBF) kernel.

Limitations with fast updates (streaming data) and large data sets. Cubic time complexity  $\mathcal{O}(N^3)$  due to matrix inversion.



$$\mathbf{A}\mathbf{w} = \mathbf{y} \quad (1)$$

$$\mathbf{A} = \mathbf{K}(\mathbf{X}, \mathbf{X}) + \sigma_n^2 \mathbf{I} \quad (2)$$

$$K_{ij} = k(\mathbf{x}_i, \mathbf{x}_j) = \sigma_F^2 e^{(-\frac{1}{2}(\mathbf{x}_i - \mathbf{x}_j)^T \mathbf{M}(\mathbf{x}_i - \mathbf{x}_j))} \quad (3)$$

$$\mathbf{R} = \text{cholesky}(\mathbf{A}) \quad (4)$$

$$\mathbf{w} = \mathbf{R} \setminus (\mathbf{R}^T \setminus \mathbf{y}) \quad (5)$$

$$\mathbf{v} = \mathbf{R}^T \setminus \mathbf{k}(\mathbf{X}, \mathbf{x}) \quad (6)$$

$$\mu(\mathbf{x}^*) = \mathbf{k}(\mathbf{x}^*, \mathbf{X}) \mathbf{w} \quad (7)$$

$$\sigma^2(\mathbf{x}^*) = k(\mathbf{x}^*, \mathbf{x}^*) - \mathbf{v}^T \mathbf{v} \quad (8)$$

Rasmussen, C. E. & Williams, C. K. I. (2006) *Gaussian processes for machine learning*. Cambridge, Mass: MIT Press.



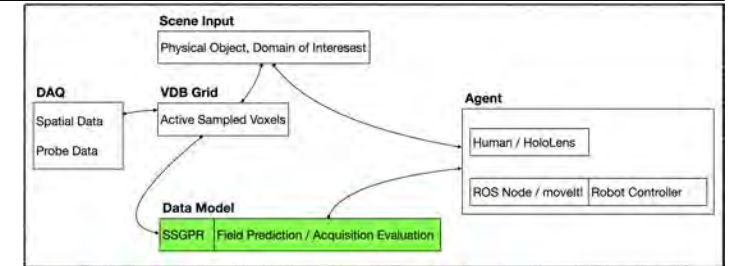
## Data Model

Model field properties:

- pressure (scalar field)
- velocity (vector field)

Sparse Spectrum Gaussian Process Regression (SSGPR).

Approximation of RBF kernel with trigonometric basis functions => covariance function with fixed size.



$$\Omega \sim 1 \mathcal{N}(\mathbf{0}, \mathbf{I}) \quad (9)$$

$$\phi(\mathbf{x}) = \frac{\sigma_f}{\sqrt{D}} \left[ \sin(\Omega \mathbf{x})^T, \cos(\Omega \mathbf{x})^T \right]^T \quad (10)$$

$$\Phi = [\phi(\mathbf{x}_1), \phi(\mathbf{x}_2), \dots, \phi(\mathbf{x}_n)] \quad (11)$$

$$\mathbf{A} = \Phi^T \Phi + \sigma_n^2 \mathbf{I} \quad (12)$$

$$\mathbf{b} = \Phi \mathbf{y} \quad (13)$$

$$\mu(\mathbf{x}^*) = \phi(\mathbf{x}^*)^T \mathbf{R} \setminus (\mathbf{R}^T \setminus \mathbf{b}) \quad (14)$$

$$\sigma^2(\mathbf{x}^*) = \sigma_n^2 + \sigma_n^2 \|\mathbf{R} \setminus \phi(\mathbf{x}^*)\|^2 \quad (15)$$

Lázaro-Gredilla, M., Quinonero-Candela, J., Rasmussen, C.E. and Figueiras-Vidal, A.R., 2010. Sparse spectrum Gaussian process regression. *The Journal of Machine Learning Research*, 11, pp.1865-1881.

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## Data Model

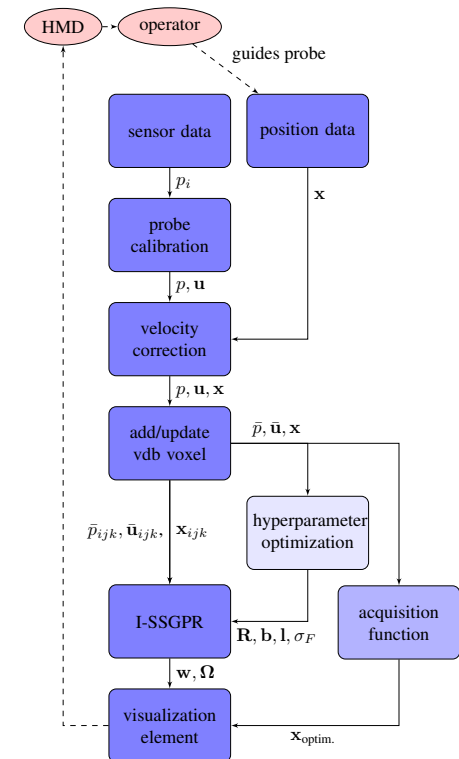
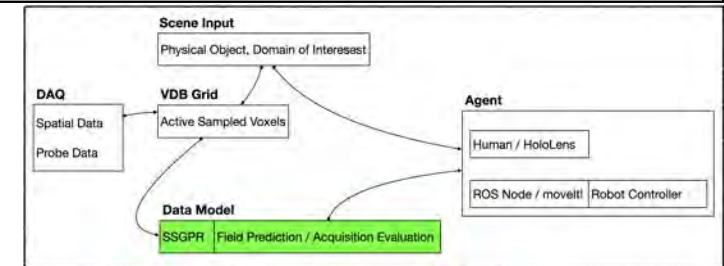
Model field properties:

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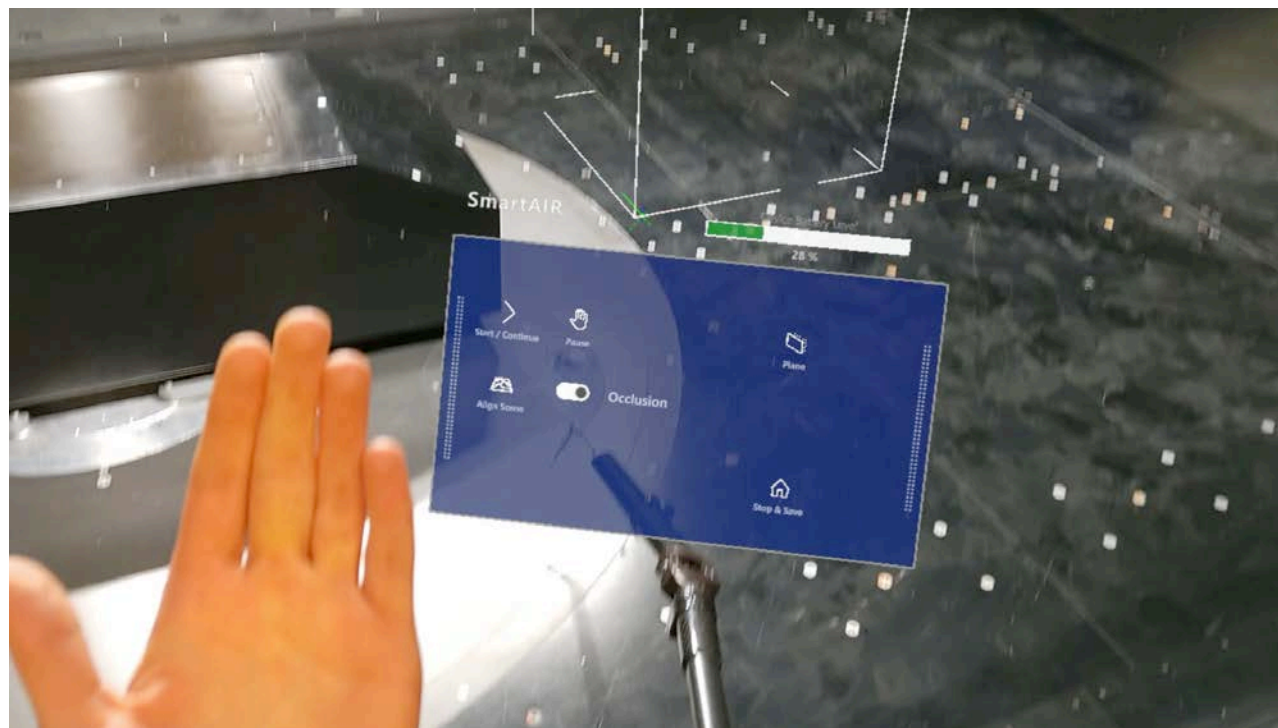
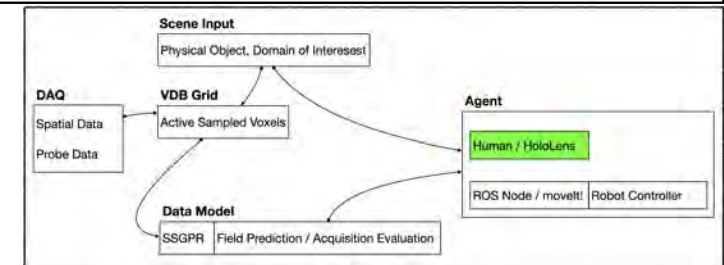
## Sparse Spectrum Gaussian Process Regression

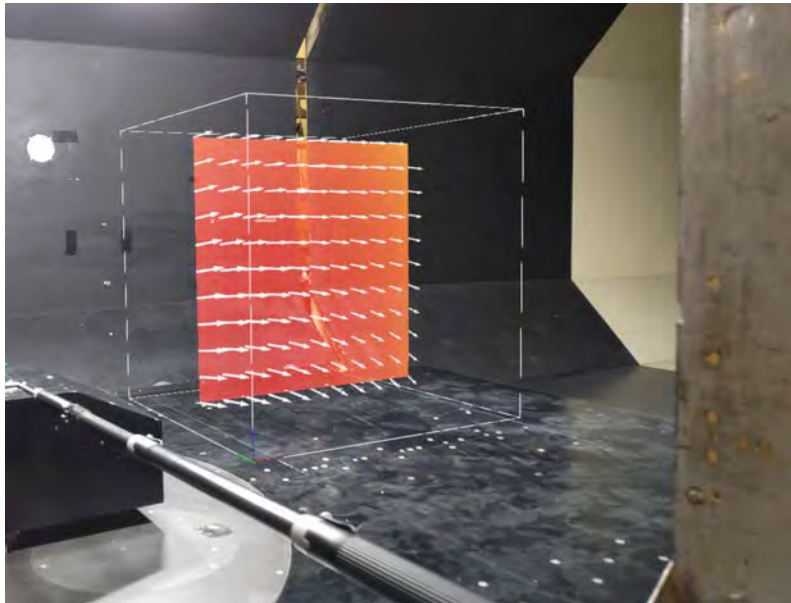
Periodically online optimization of sparse kernel  
Hyperparameters with neg. log. marginal likelihood. Combining  
SSGPR and Iterative-SSGPR allows for minimal prior knowledge.  
Implemented via PyTorch C++ Interface.

=> goal to still run on portable computer (Laptop)...

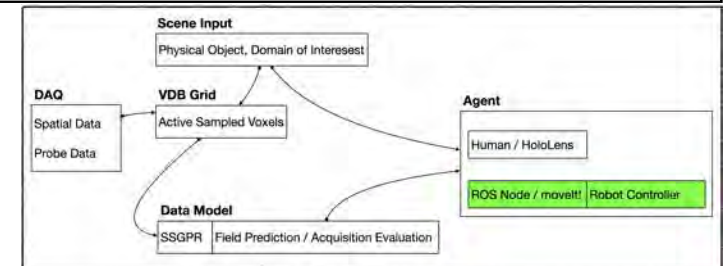


## Human Agent / HoloLens

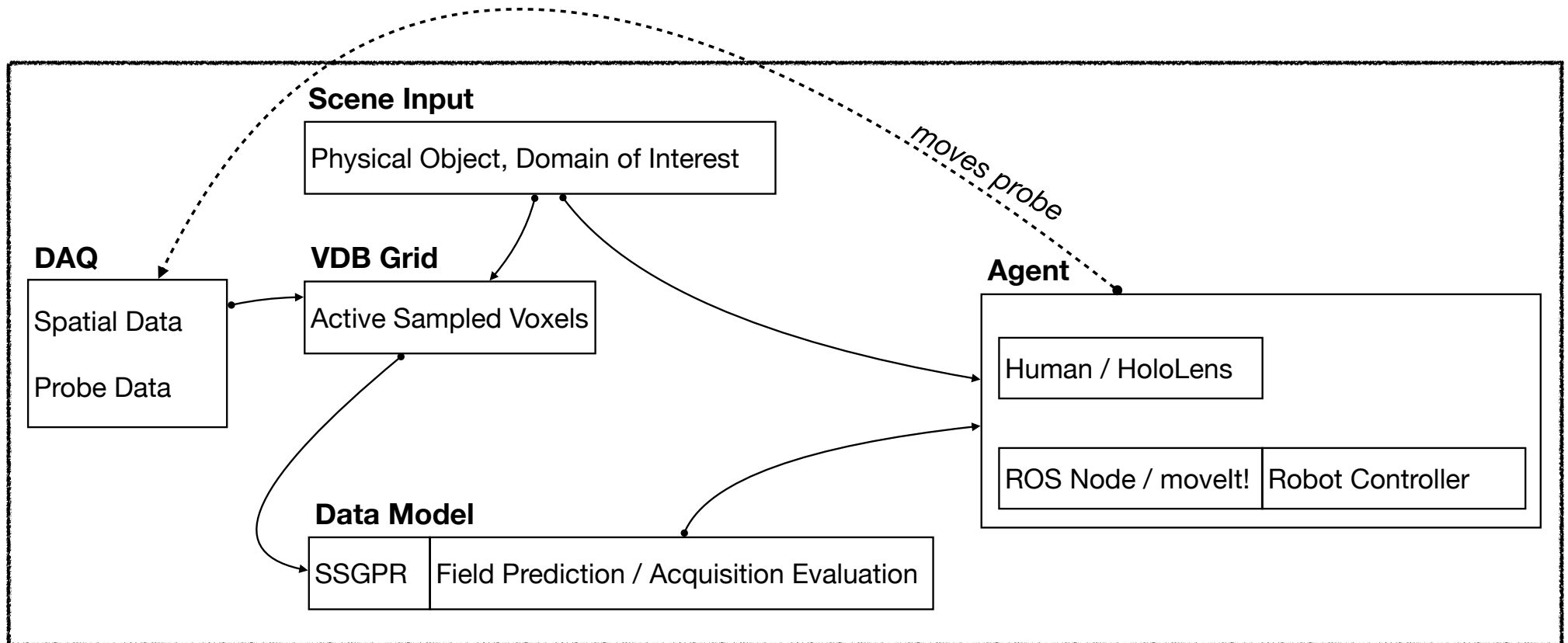


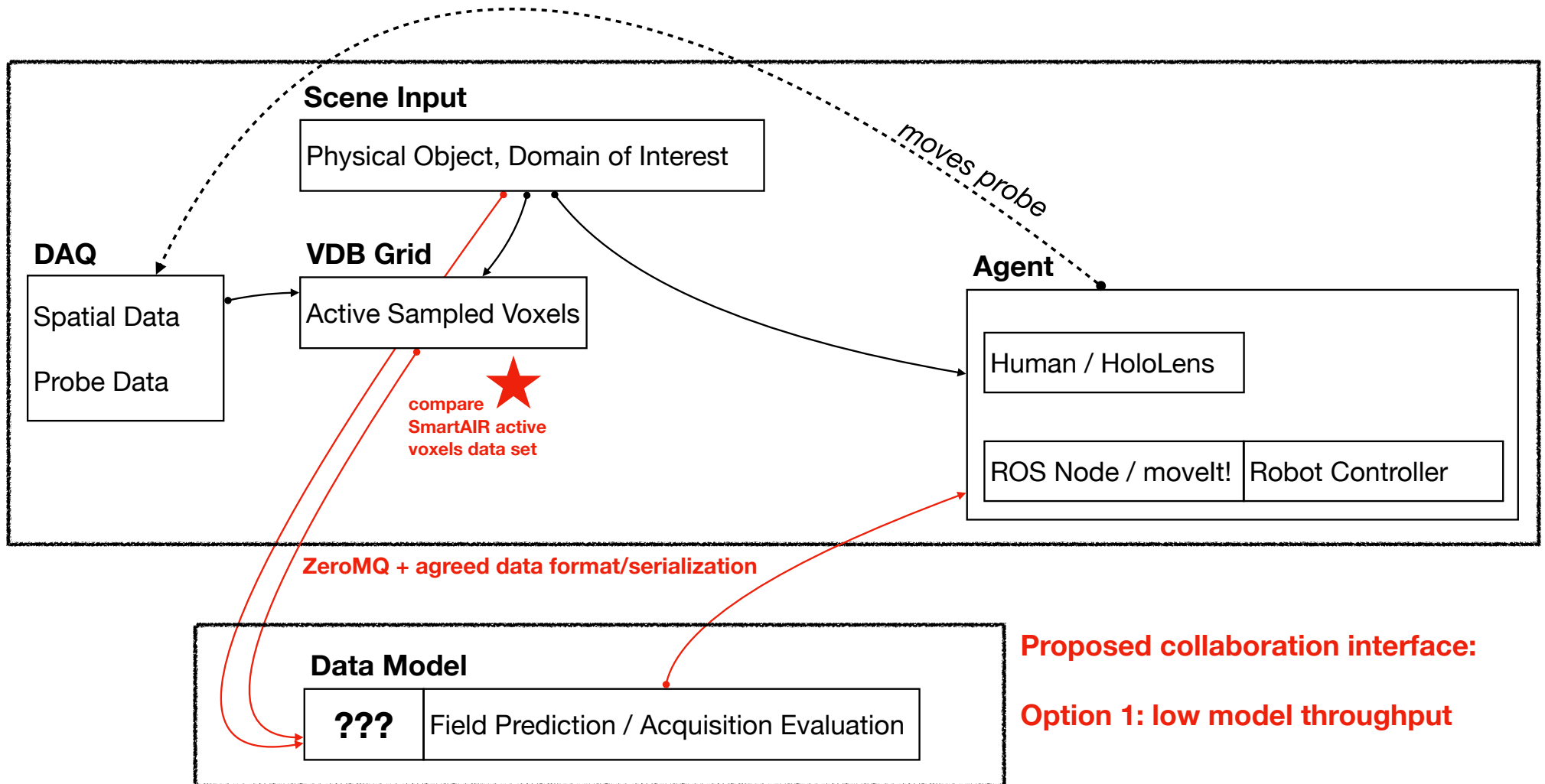


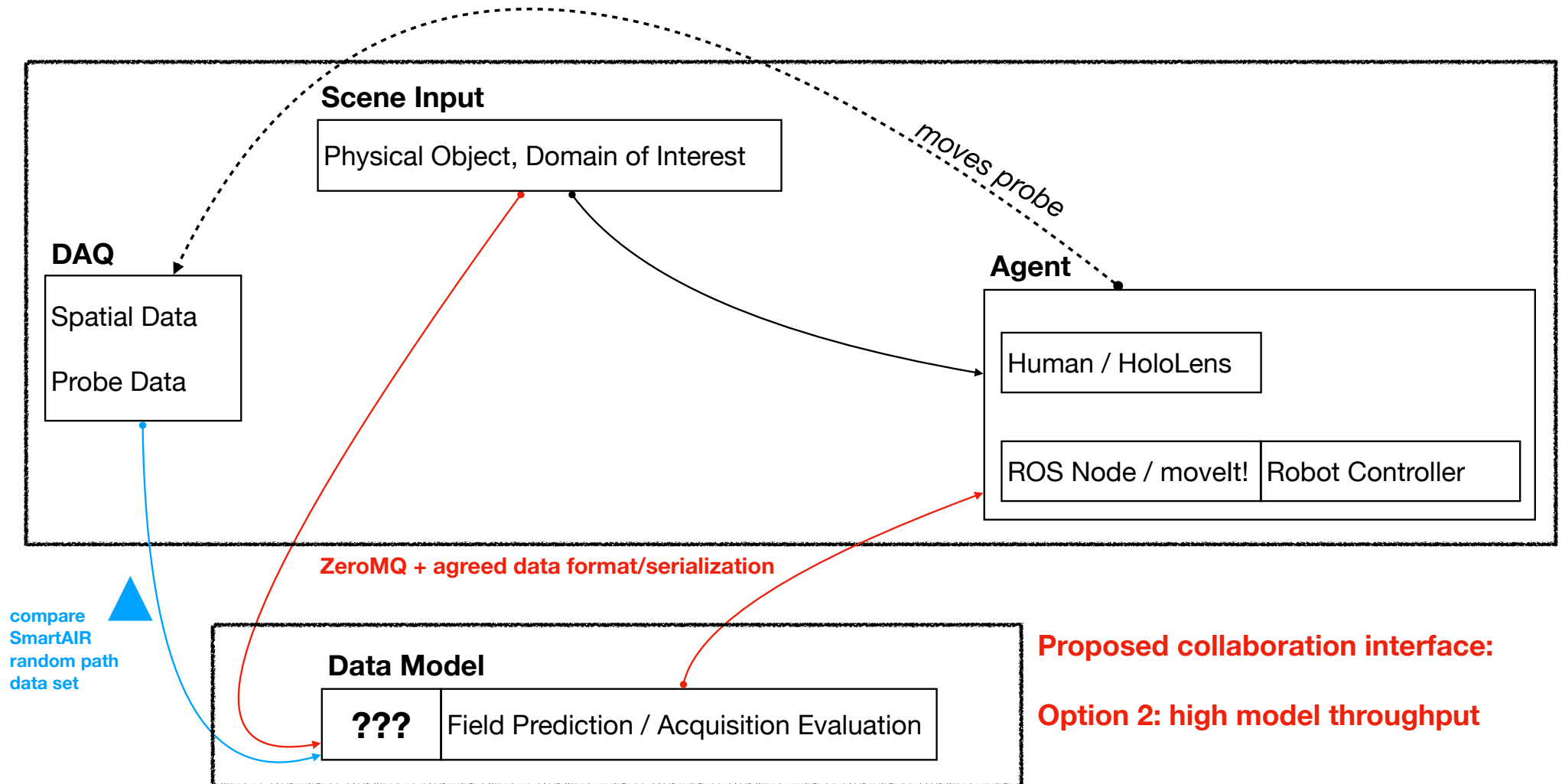
## Robotic Agent











## Data Sets Available

### A. Wind Tunnel Measurements

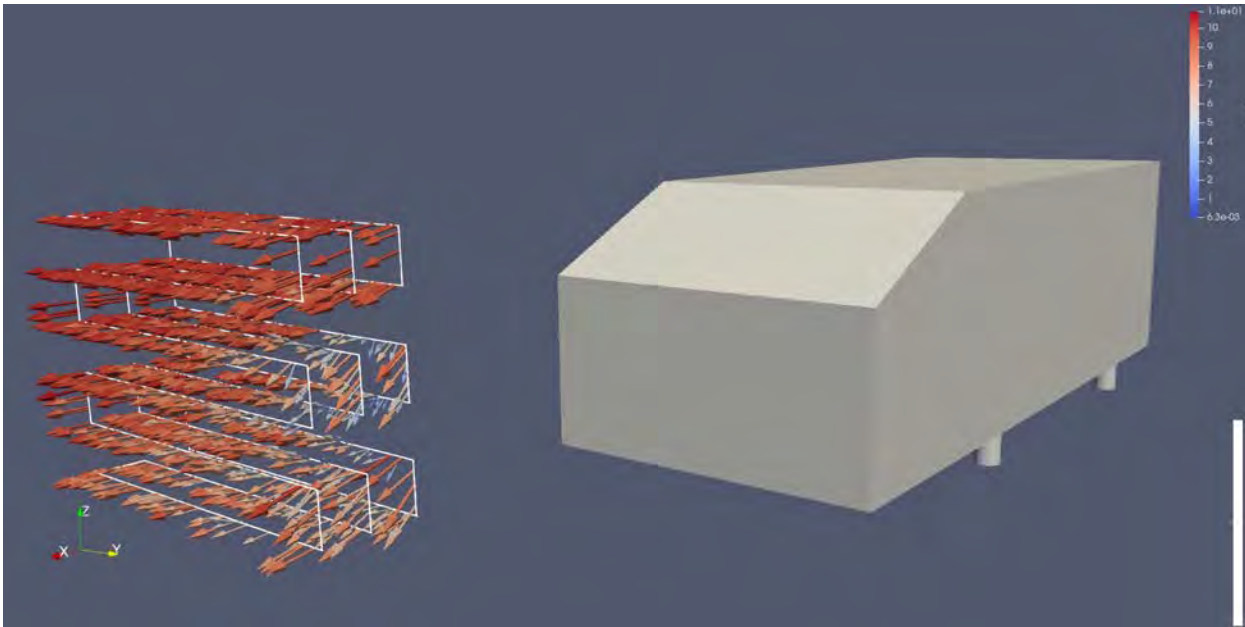
- i. Ahmed Body Traverse
- ii. Ahmed Body SmartAIR “random” path

### B. Computational Fluid Dynamics (CFD) Simulations

- i. Ahmed Body (3D / stationary)
- ii. Von Kármán Vortex Shedding (2D / non stationary)

## Data sets available

### A.i.) Ahmed Body Traverse Measurement



#### Project motivation:

Measurement took 25 minutes.  
Measure the actual flow, sparse data.  
Difficult to visualize and post process.

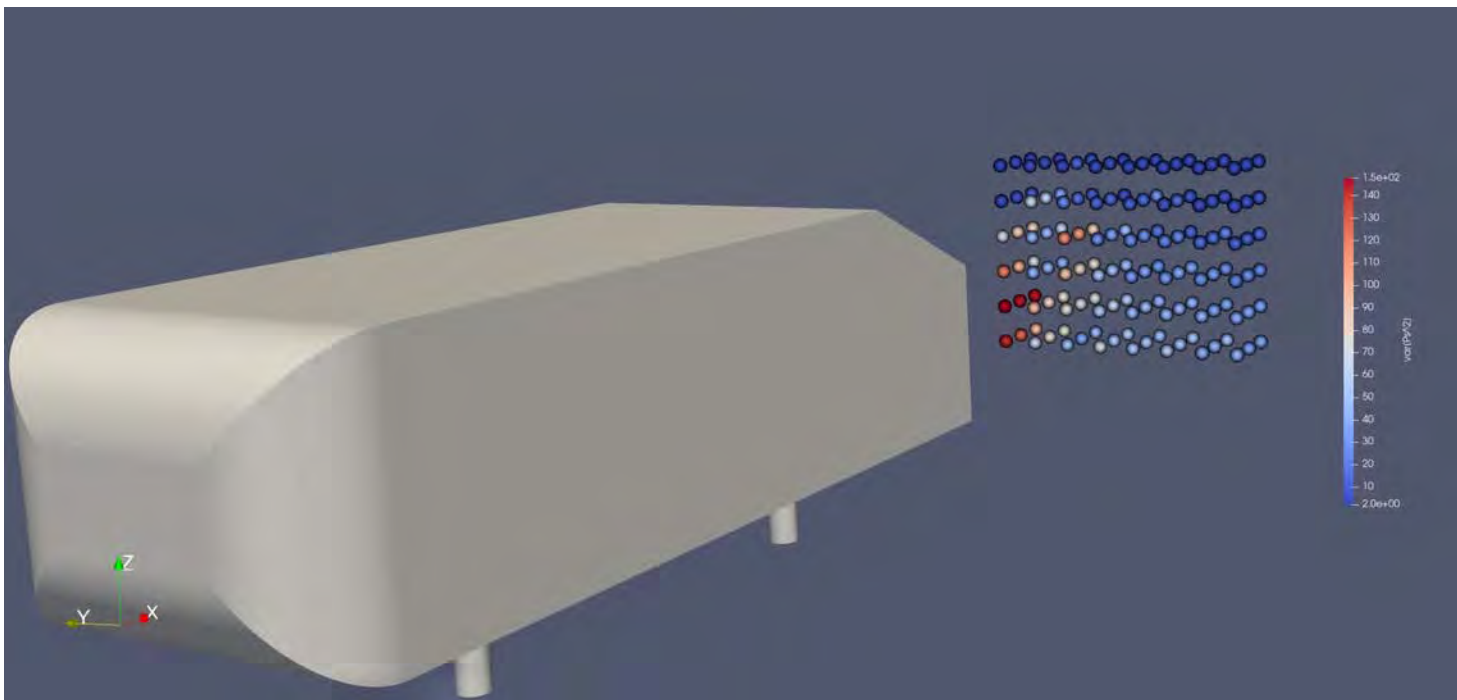
Compare corresponding CFD case.  
Rich data allows extensive post  
processing. Very difficult to get the  
physics right.

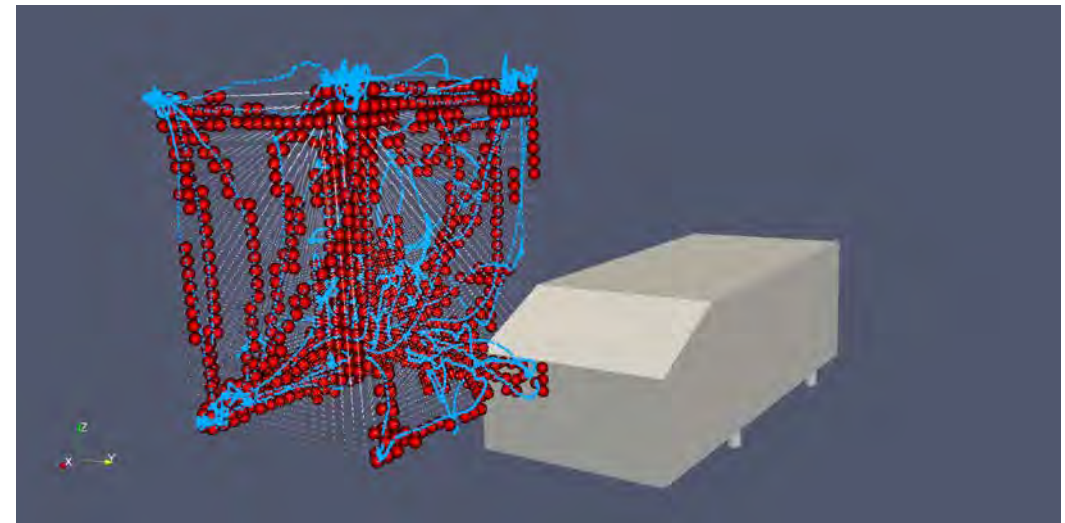
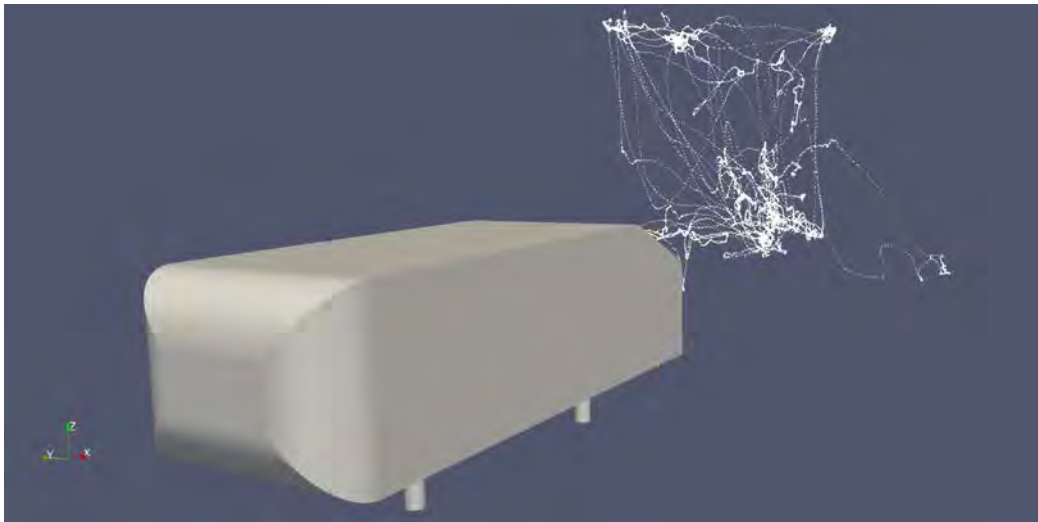
SmartAIR => short measurement time  
with data richness comparable to CFD.

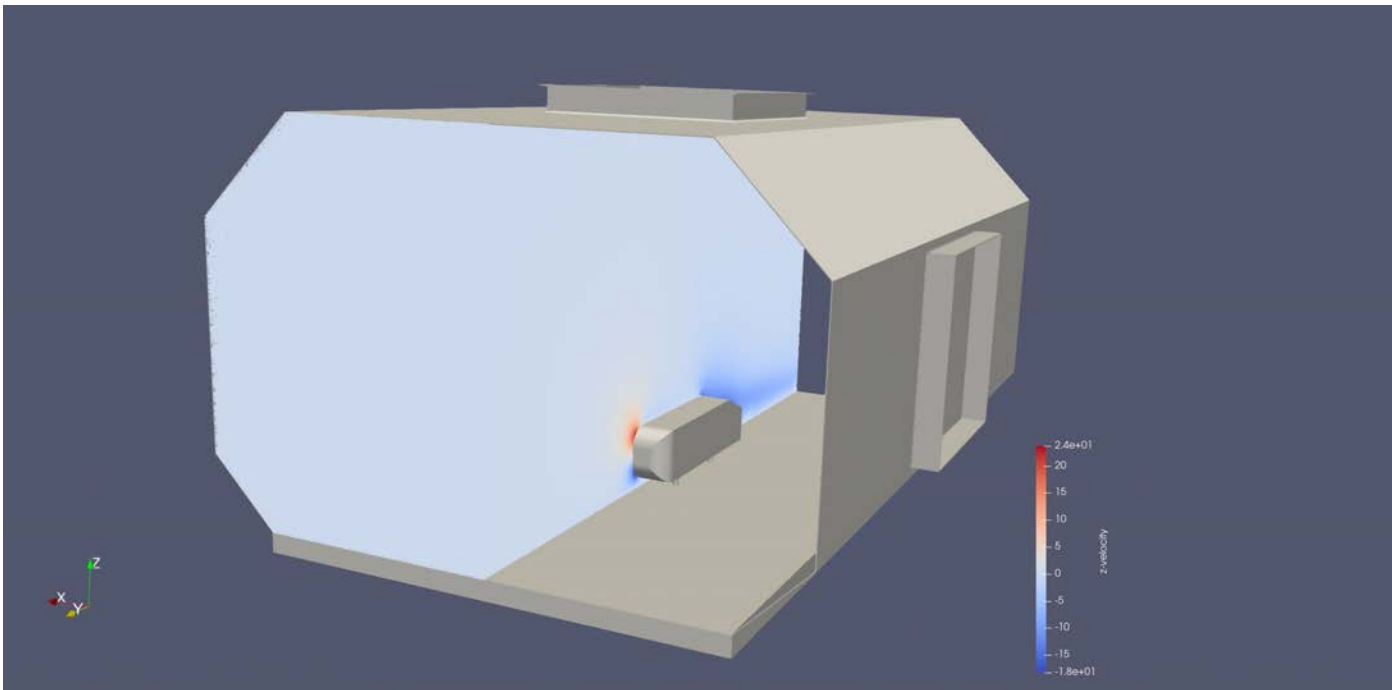


## Data sets available

### A.i.) Ahmed Body Traverse Measurement — Variance Field

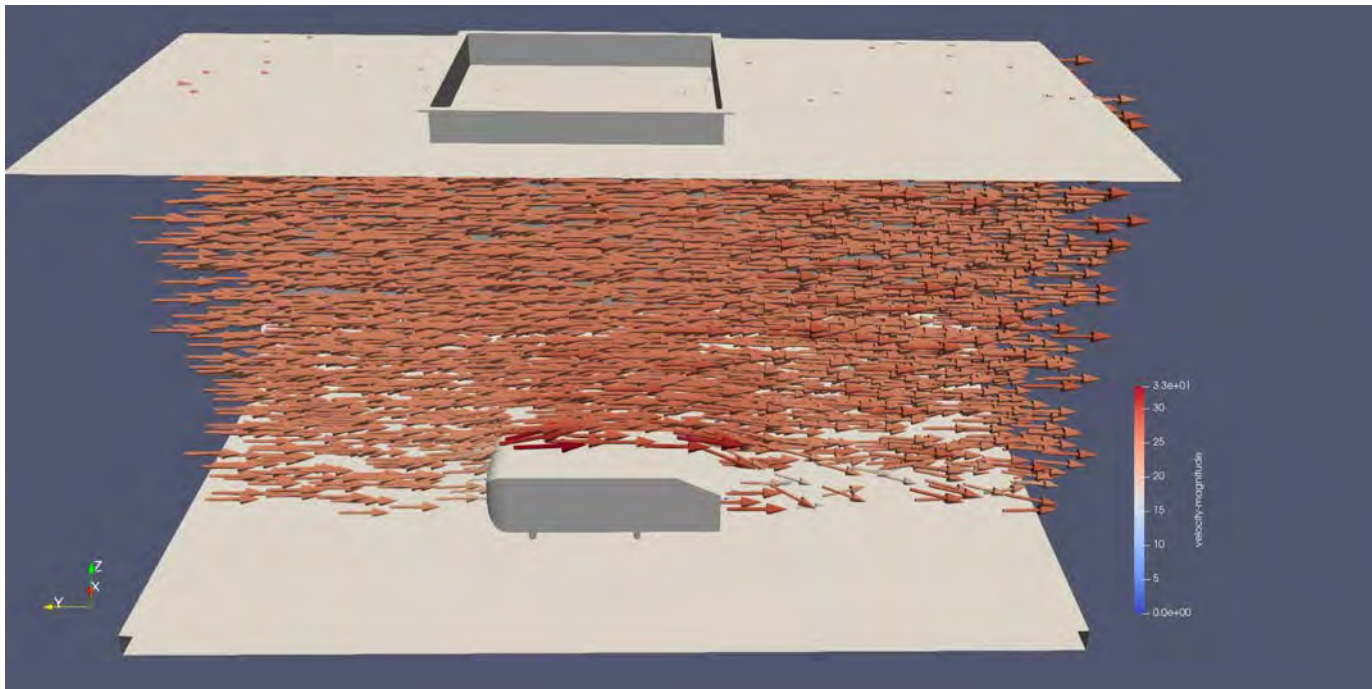


Data sets availableA.ii.) Ahmed Body SmartAIR random path

Data sets availableB.i.) Ahmed Body CFD

## Data sets available

### B.i.) Ahmed Body CFD



#### Project motivation:

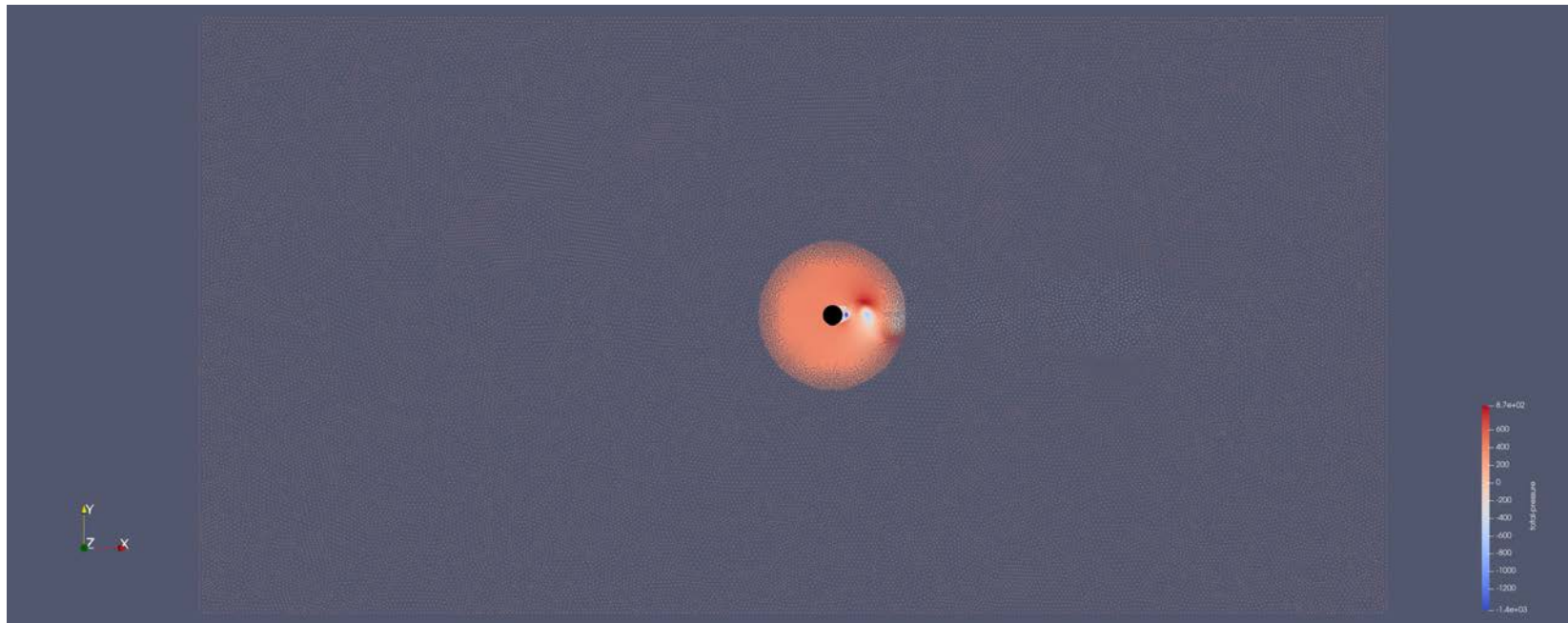
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Data sets available

B.ii.) Von Kármán Vortex Street





Data sets available

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# Questions and Discussion.



## References:

Müller, A. (2017) Real-Time 3D Flow Visualization Technique with Large Scale Capability. ETH Zurich; Zurich.

Rasmussen, C. E. & Williams, C. K. I. (2006) *Gaussian processes for machine learning* . Cambridge, Mass: MIT Press.

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