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## Geometry (Intermediate)

## Use the information below to answer questions 1-3.

In the diagram below, $\overline{B D} \| \overline{A E}$ and $\overline{A B} \| \overline{C D}$ and $\triangle C D E$ is equilateral.


1. What is the perimeter of $C B D E$ ?
A. 24
B. 28
C. 34
D. $8+\frac{40 \sqrt{3}}{3}$
E. $8+40 \sqrt{3}$
2. What is the area of $A B D C$ ?
A. 16
B. 24
C. 32
D. 48
E. 60
3. What is the sum of $\mathrm{m} \angle E D C$ and $\mathrm{m} \angle B C E$ in degrees?
A. $120^{\circ}$
B. $145^{\circ}$
C. $150^{\circ}$
D. $160^{\circ}$
E. $170^{\circ}$
4. The equilateral triangle $\triangle A B C$ is shown to the right. $\overline{B D}$ is the perpendicular bisector of $\overline{A C}$, and $\overline{B D}$ measures $8 \sqrt{3}$ inches. What is the perimeter of $\triangle A B C$ in inches?
A. 16
B. 24
C. $24 \sqrt{3}$
D. 48
E. $64 \sqrt{3}$

5. In the figure below, $\triangle A B C \sim \triangle E F G$, sides $\overline{E F}$ and $\overline{F G}$ are both 4.8 cm long, side $\overline{A B}$ is 9.6 cm long, and the measure of $\angle A B C$ is $45^{\circ}$. What is the measure of $x$ ?

A. $60^{\circ}$
B. $65^{\circ}$
C. $67.5^{\circ}$
D. $72.5^{\circ}$
E. $75^{\circ}$
6. In the diagram to the right, $\overline{\mathrm{CB}}$ is tangent to circle $A$ at point $B$, and $\angle C A B=56.49^{\circ}$. What is the measure of $\angle \mathrm{ACB}$ to the nearest degree?
A. $23^{\circ}$
B. $29^{\circ}$
C. $34^{\circ}$
D. $37^{\circ}$
E. $45^{\circ}$

7. The height of the triangle to the right is 12 units. What is its area in square units?
A. 72
B. 84
C. 168
D. 240
E. Cannot be determined from the given information

8. An angle is bisected, and each of the resulting angles is trisected. The final angle measure of each resulting angle is $12.5^{\circ}$. What was the measure of the original angle?
A. $58^{\circ}$
B. $65^{\circ}$
C. $72^{\circ}$
D. $75^{\circ}$
E. $82^{\circ}$
9. In the figure to the right, $\overline{X Z}$ is the perpendicular bisector of $\triangle W X Y$, and $\overline{W Y}=24$. What is the ratio of the area to the perimeter of $\triangle W X Y$ ?
A. 6: 5
B. $4: 3$
C. 3: 5
D. 2:3
E. 1:2

10. How much larger is the smallest angle created by the hour and minute hand at 7:00 than the smallest angle created by the hour and minute hand at $1: 00$ ?
A. $100^{\circ}$
B. $120^{\circ}$
C. $130^{\circ}$
D. $140^{\circ}$
E. $150^{\circ}$


Use the information below to answer questions 11-12


In the diagram, $\triangle A B C$ is inscribed between two overlapping circles with center points $A(3,2)$ and $B(7,2) . \triangle A B C$ is an equilateral triangle.
11. What is the circumference of the circle with center point

A?
A. $4 \pi$
B. $8 \pi$
C. $12 \pi$
D. $14 \pi$
E. $16 \pi$
12. What is the length of the arc between points $B$ and $C$ on circle $A$ ?
A. $\frac{1}{2} \pi$
B. $\pi$
C. $\frac{4}{3} \pi$
D. $2 \pi$
E. $4 \pi$
13. In the figure to the right, $\triangle A B C$ is an equilateral triangle. $\overleftrightarrow{A B} \| \overleftrightarrow{E F}$, E bisects $\overleftrightarrow{A C}$ and $F$ bisects $\overleftrightarrow{B C}$. What is the ratio of the area of $\triangle E F C$ to that of $\triangle A B C$ ?
A. $1: 4$
B. 1:3
C. $1: 1$
D. 2: 1
E. 2: 3
14. A circle is inscribed in a square, which has a perimeter
 of 40 cm . What is the area of the circle?
A. $10 \pi$
B. $25 \pi$
C. $40 \pi$
D. $50 \pi$
E. $100 \pi$
15. Point $R$ exists at some distance from a circle. Lines are drawn from point $R$ and run tangent to the circle at points $P$ and $Q$. If $\angle P R Q$ is $50^{\circ}$, what is the measure of $\angle \mathrm{RPQ}$ ?
A. $50^{\circ}$
B. $60^{\circ}$
C. $65^{\circ}$
D. $70^{\circ}$
E. $75^{\circ}$
16. Two cylinders both have a height of 4 , but the first cylinder has a radius of 3 , and the second has a radius of 5. What is the ratio of the volume of these cylinders?
A. 3: 5
B. 7: 9
C. $9: 25$
D. 4:5
E. 27: 125
17. In $\triangle A B C, \overline{A B}=5 \mathrm{~cm}, \overline{A C}=10 \mathrm{~cm}, m \angle \mathrm{~A}=60$, and $\overline{A C}$ is the longest side. Which of the following statements about the measures of the angles in $\triangle A B C$ must be true?
A. $m \angle A=m \angle B=m \angle C$
B. $m \angle B>m \angle A>m \angle C$
C. $m \angle B=m \angle C>m \angle A$
D. $m \angle B>m \angle C=m \angle A$
E. $m \angle C>m \angle A>m \angle B$
18. Given the circle below with $A B=6$, and $\angle B A C=60^{\circ}$ find the length of arc $B C$.
A. $\frac{\pi}{6}$
B. $\frac{\pi}{2}$
C. $\pi$
D. $2 \pi$
E. $6 \pi$

19. A 5-inch-by-5-inch square grid shown below is divided into 25 squares, each with a side length of 1 inch. Each vertex of the two shaded triangles lies at an intersection of 2 grid lines. What fractional part of the 5-inch-by-5inch square is shaded?

A. $\frac{1}{3}$
B. $\frac{9}{25}$
C. $\frac{1}{2}$
D. $\frac{3}{5}$
E. $\frac{3}{4}$
20. What is the perimeter of an isosceles right triangle with hypotenuse $5 \sqrt{2}$ feet long?
A. 10
B. 15
C. $5+5 \sqrt{2}$
D. $10+5 \sqrt{2}$
E. $15+5 \sqrt{2}$
21. In quadrilateral $A B C D$ shown below, $\overline{A D} \| \overline{B C}, B C=$ 18 centimeters, $A D=26$ centimeters, and the distance between $\overline{A C}$ and $\overline{A C}$ is 6 centimeters. What is the area, in square centimeters, of quadrilateral $A B C D$ ?

A. 108
B. 132
C. 156
D. 264
E. 468

